

Podobno zo spojitosli $\psi(x)$ a $d\psi(x)/dx$ v bode $x=a$

$$F e^{-\alpha a} = C \sin(\beta a) + D \cos(\beta a) \quad (3)$$

$$-\alpha F e^{-\alpha a} = C \cos(\beta a) - D \sin(\beta a) \quad (4)$$

$$(3)-(1) (F-B) e^{-\alpha a} = 2C \sin(\beta a) \quad (5)$$

$$(4)-(2) \alpha(F-B) e^{-\alpha a} = 2\beta C \cos(\beta a) \quad (6)$$

$$(3)+(1) (B+F) e^{-\alpha a} = 2D \cos(\beta a) \quad (7)$$

$$(2)-(4) \alpha(B+F) e^{-\alpha a} = 2D\beta \sin(\beta a) \quad (8)$$

Mame dva typy riešení!

- ① Ak $C=0$ a $F=B \Rightarrow$ (5) a (6) platia identicky a z (7) a (8) dostaneme

$$\frac{2\beta D \sin(\beta a)}{2D \cos(\beta a)} = \frac{\alpha(B+F) e^{-\alpha a}}{(B+F) e^{-\alpha a}}$$

$$\boxed{\beta = \tan(\beta a) = \alpha} \quad (9)$$

- ② Ak $D=0$ a $B=-F \Rightarrow$ (7) a (8) platia identicky a z (5) a (6) mame

$$\frac{-\alpha(F-B) e^{-\alpha a}}{(F-B) e^{-\alpha a}} = \frac{2\beta C \cos(\beta a)}{2C \sin(\beta a)}$$

$$\boxed{-\alpha = \beta \cot(\beta a)} \quad (10)$$

Riešime (9) geometricky (transcendenciou)
Položime:

$$\xi = \beta a \quad \eta = \alpha a$$

$$\Rightarrow \xi^2 + \eta^2 = a^2 (\beta^2 + \alpha^2) =$$

$$= a^2 \frac{2m}{\hbar^2} [E + V_0 - E] = \frac{2m}{\hbar^2} V_0 a^2 = R^2$$